

CAMBRIDGE INTERNATIONAL EXAMINATIONS
International General Certificate of Secondary Education

MARK SCHEME for the October/November 2013 series

0580 MATHEMATICS

0580/42

Paper 4 (Extended), maximum raw mark 130

This mark scheme is published as an aid to teachers and candidates, to indicate the requirements of the examination. It shows the basis on which Examiners were instructed to award marks. It does not indicate the details of the discussions that took place at an Examiners' meeting before marking began, which would have considered the acceptability of alternative answers.

Mark schemes should be read in conjunction with the question paper and the Principal Examiner Report for Teachers.

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Abbreviations

| | |
|-----|----------------------------|
| cao | correct answer only |
| cso | correct solution only |
| dep | dependent |
| ft | follow through after error |
| isw | ignore subsequent working |
| oe | or equivalent |
| SC | Special Case |
| www | without wrong working |
| art | anything rounding to |
| soi | seen or implied |

| | Correct answer | Mark | Part marks |
|----------|---|---|---|
| 1 | <p>(a) (i) 3216 Final answer</p> <p>(ii) 1307 Final answer</p> <p>(b) 4.5[%] nfw</p> <p>(c) A by 31.05... or 31.04 to 31.05 or 31.[0] 31.1[0]</p> | <p>2</p> <p>2FT</p> <p>2</p> <p>5</p> | <p>M1 for $(18900 - 5500) \times 0.24$ oe</p> <p>FT $(18900 - \text{their (a)(i)}) \div 12$ correctly evaluated</p> <p>M1 for $(18900 - \text{their (a)(i)}) \div 12$</p> <p>M1 for $\frac{19750.50[-18900]}{18900} \times 100$ or $\frac{19750.50 - 18900}{18900}$</p> <p>M1 for $1500 \times 4.1/100 \times 3$ [+ 1500] oe M1 for 1500×1.033^3 [- 1500] oe A1 for 1684.5 or 184.5 or 1653[.45..] or 153[.45..]</p> <p>and M1dep for subtraction of <i>their</i> amounts or <i>their</i> interests</p> |
| 2 | <p>(a) 36.9° or 36.86 to 36.87</p> <p>(b) (i) $1.8^2 + 2.4^2$ leading to $\sqrt{9}$</p> <p>(ii) $[\cos ABD] = \frac{6.46^2 + 3^2 - 8.6^2}{2 \times 6.46 \times 3}$ 127 or 126.8...</p> <p>(c) 39.6 or 39.7 or 39.59 to 39.68</p> | <p>2</p> <p>2</p> <p>M2</p> <p>A2</p> <p>3</p> | <p>M1 for $\tan[DBC] = 1.8/2.4$ oe</p> <p>M1 for $1.8^2 + 2.4^2$ or better</p> <p>M1 for correct cos rule but implicit version</p> <p>A1 for -0.599...</p> <p>After 0 scored, SC2 nfw for answer 127 or 126.8 to 126.96 from other methods or no working shown</p> <p>M2 for $\frac{1}{2}(2.4 + 8.6) \times 1.8 \times 4$ oe Or M1 for $\frac{1.8}{2}(2.4 + 8.6)$ oe soi by 9.9 to 9.92</p> |

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|---|---|------------------------------|---|
| 3 | <p>(a) $\frac{4x-7}{10}$ final answer nfw</p> <p>(b) $x^2 + 9$ final answer nfw</p> <p>(c) (i) $(2x-1)(x+3)$ isw solving</p> <p>(ii) $\frac{2x-1}{2(x-3)}$ or $\frac{2x-1}{2x-6}$ final answer nfw</p> | 3 4 2 3 | <p>M2 for $\frac{5(2x-1)-2(3x+1)}{2 \times 5}$ or $\frac{5(2x-1)}{5 \times 2} - \frac{2(3x+1)}{5 \times 2}$ or M1 for attempt to convert to common denominator of 10 or multiple of 10 with one error in numerator</p> <p>B3 for $4x^2 - 6x - 6x + 9 - 3x^2 + 12x$ or correct answer given and then spoilt or B1 for $4x^2 - 6x - 6x + 9$ seen and B1 for $-3x^2 + 12x$ or $-(3x^2 - 12x)$ seen</p> <p>M1 for $(2x+a)(x+b)$ where $ab = -3$ or $2b + a = 5$ with integers a and b</p> <p>M2 for $2(x+3)(x-3)$ or $(2x-6)(x+3)$ or $(2x+6)(x-3)$ seen or M1 for $2(x^2-9)$ seen</p> |
| 4 | <p>(a) (i) $90 \div (42/360 \times \pi \times 8^2)$ o.e. 3.836 to 3.837</p> <p>(ii) 131 or 130.75 to 130.9 nfw</p> <p>(b) 2.42 or 2.416 to 2.419</p> | M3 A1 5 3 | <p>M2 for $42/360 \times \pi \times 8^2 \times h = 90$ or M1 for $42/360 \times \pi \times 8^2$</p> <p>M2 for $42/360 \times \pi \times 2 \times 8 \times 3.84$ oe [22.48 to 22.53] or M1 for $42/360 \times \pi \times 2 \times 8$ oe soi [5.86 to 5.87] and M1 for $2 \times (8 \times 3.84)$ [61.37 to 61.44] and M1 for $2 \times (42/360 \times \pi \times 8^2)$ [46.88 to 47]</p> <p>M2 for $3.84 \times \sqrt[3]{\frac{22.5}{90}}$ oe or $h = \sqrt[3]{\frac{3.84^3 \times 22.5}{90}}$</p> <p>or M1 for $\sqrt[3]{\frac{22.5}{90}}$ oe or $\sqrt[3]{\frac{90}{22.5}}$ oe seen</p> <p>or $\frac{3.84^3}{h^3} = \frac{90}{22.5}$ oe</p> |

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| 5 | (a) 7, 11.5, 4.5 | 1,1,1 | |
| | (b) Correct curve cao | 5 | B3FT for 10 correct plots, on correct vertical grid line and within correct 2 mm square vertically Or B2FT for 8 or 9 correct plots Or B1FT for 6 or 7 correct plots and B1 indep for two separate branches on either side of y -axis |
| | (c) (i) $0.69 < x < 0.81$ | 1 | |
| | (ii) $-2.3 < x < -2.2$ $-0.8 < x < -0.6$ $0.35 < x < 0.5$ | 3 | B1 for each correct After 0 scored, allow SC1 for drawing line $y = 7.5$ long enough to cross curve at least once |
| | (d) (i) $y = 10 - 3x$ ruled correctly | B2 | long enough to cross curve twice. B1 for ruled line gradient -3 or y intercept at 10 but not $y = 10$ Or B1 for 'correct' but freehand |
| | $-0.55 < x < -0.45$ $0.35 < x < 0.45$ | B1dep B1dep | Dependent on at least B1 scored for line After 0 scored, SC2 for -0.5 and 0.4 [from solving equation] |
| | (ii) $\begin{matrix} 10 & 1 & -2 \\ \text{or} & -10 & -1 & 2 \end{matrix}$ | 3 | B2 for $2 - x - 10x^2 [= 0]$ oe Or B1 for $\frac{2}{x^2} - \frac{1}{x} - 10 = 0$ oe Correctly eliminating $-3x$ Or B1 for $2 - x - 3x^3 = 10x^2 - 3x^3$ oe Correctly clearing fractions |

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| 6 | (a) (i) | $\frac{1}{110}$ oe | | 2 | M1 for $\frac{1}{11} \times \frac{1}{10}$ |
| | (ii) | $\frac{6}{110}$ oe | $\left[\frac{3}{55} \right]$ | 2 | M1 for $\frac{3}{11} \times \frac{2}{10}$ |
| | (iii) | $\frac{8}{110}$ oe | $\left[\frac{4}{55} \right]$ | 2FT | FT their (a)(ii) + $\frac{2}{11} \times \frac{1}{10}$ correctly evaluated or M1 their (a)(ii) + $\frac{2}{11} \times \frac{1}{10}$ |
| | (b) (i) | $\frac{6}{990}$ oe | $\left[\frac{1}{165} \right]$ | 2 | M1 for $\frac{3}{11} \times \frac{2}{10} \times \frac{1}{9}$ |
| | (ii) | $\frac{336}{990}$ oe | $\left[\frac{56}{165} \right]$ | 2 | M1 for $\frac{8}{11} \times \frac{7}{10} \times \frac{6}{9}$ |
| | (iii) | $\frac{198}{990}$ oe | $\left[\frac{1}{5} \right]$ | 5 | M4 for $3\left(\frac{3}{11} \times \frac{2}{10} \times \frac{8}{9}\right) + 3\left(\frac{2}{11} \times \frac{1}{10} \left[\times \frac{9}{9}\right]\right)$ oe or M3 for $3\left(\frac{3}{11} \times \frac{2}{10} \times \frac{8}{9}\right)$ or $3\left(\frac{2}{11} \times \frac{1}{10} \left[\times \frac{9}{9}\right]\right)$ oe Or M1 for $\frac{3}{11} \times \frac{2}{10} \times \frac{8}{9}$ oe seen and M1 for $\frac{2}{11} \times \frac{1}{10} \left[\times \frac{9}{9}\right]$ oe seen |

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| 7 | (a) 14 10 or 2 10 pm final answer | 2 | M1 for (0)8 10 oe or answer 14 hours and 10 minutes or answer 2 10 [am] |
| | (b) 5 hours 45 minutes cao | 2 | M1 for 345 [mins] seen or for $805 / 7 \times 3$ oe or 5.75 seen |
| | (c) (i) 798 or 798.2 to 798.4.... | 2 | M1 for $10712 / 13 \frac{25}{60}$ or $10712 \div 13.4\dots$ |
| | (ii) 1.82×10^5 or 1.815×10^5 to 1.816×10^5 | 4 | B3 for 182000 or 181500 to 181600 seen or M2 for 10712000/59 oe or M1 for figs 10712/figs 59 soi by figs 182 or figs 1815 to 1816 and B1 FT for their number of litres correctly converted to standard form rounded to 3sf or better |
| (d) 8600 | 3 | M2 for $10148 \div 1.18$ oe or M1 for 10148 associated with 118[%] | |
| 8 | (a) (i) -6 | 1 | |
| | (ii) 2.75 oe | 2 | M1 for [g(x) =] 0.5 or 7/14 Or $\left(\frac{7}{x+1}\right)^2 + 5\left(\frac{7}{x+1}\right)$ oe |
| | (b) $\frac{x-3}{4}$ or $\frac{x}{4} - \frac{3}{4}$ Final answer | 2 | M1 for $y - 3 = 4x$ or better or $x = 4y + 3$ or better or $\frac{y}{4} = \frac{3}{4} + x$ or flowchart with - 3 then $\div 4$ |
| | (c) (i) 5 | 2 | M1 for $4x = 23 - 3$ or $x + \frac{3}{4} = \frac{23}{4}$ or better |
| | (ii) $x^2 + 5x - 7 = 0$ $\frac{-5 \pm \sqrt{5^2 - 4(1)(-7)}}{2(1)}$ oe | B1 B1 B1 | May be implied by correct values in formula B1 for $\sqrt{5^2 - 4(1)(-7)}$ or better [53] If in form $\frac{p + \sqrt{q}}{r}$ or $\frac{p - \sqrt{q}}{r}$, B1 for -5 and 2(1) or better No recovery of full line unless seen |
| | 1.14 and -6.14 final answers | B1 B1 | Or SC1 for 1.1 or 1.140.... and -6.1 or -6.140 ... Or answers -1.14 and 6.14 |

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| 9 | (a) (i) Reflection $x = -2$ oe | 2 | B1 for either |
| | (ii) Translation $\begin{pmatrix} -7 \\ 2 \end{pmatrix}$ oe | 2 | B1 for either |
| | (iii) Stretch x -axis oe invariant [factor] 3 | 3 | B1 for each |
| | (b) (i) Triangle with coords at (8, 2) (7, 3) and (7, 5) | 2 | B1 for rotation about (6, 0) but 90° anticlockwise Or for rotation 90° clockwise around any point |
| | (ii) Triangle with coords at (-2, -5) (-6, -5) and (-8, -7) | 2 | B1 for 2 correct points or for enlargement of SF -2 any centre |
| (iii) Triangle with coords at (1, -1) (4, -6) and (3, -5) | 2 | B1 for 2 correct points or coordinates of 2 points shown | |
| (c) $\begin{pmatrix} 1 & 0 \\ -2 & 1 \end{pmatrix}$ | 2 | B1 for one row or one column correct but not identity matrix. Or SC1 for $\begin{pmatrix} 1 & -2 \\ 0 & 1 \end{pmatrix}$ | |
| 10 | (a) 48 and 57, $9n + 3$ oe | 1 2 | B1 for $9n + k$ oe |
| | (b) 56 and 50, $86 - 6n$ oe | 1 2 | B1 for $k - 6n$ oe |
| | (c) 125 and 216, n^3 oe | 1 1 | |
| | (d) 130 and 222 $n^3 + n$ oe | 1 1FT | FT <i>their</i> (c) + n dep on expression in n in (c) |